Support for Public Provision of a Private Good with Top-Up and Opt-Out: A Controlled Laboratory Experiment

Neil Buckley\textsuperscript{a}, Katherine Cuff\textsuperscript{1,b,1}, Jeremiah Hurley\textsuperscript{b,c}, Stuart Mestelman\textsuperscript{b}, Stephanie Thomas\textsuperscript{b}, David Cameron\textsuperscript{b,c}

\textsuperscript{a}Department of Economics, York University, 4700 Keele Street, Toronto, ON, Canada, M3J 1P3
\textsuperscript{b}Department of Economics, McMaster University, 1280 Main Street West, Hamilton, ON, Canada, L8S 4M4
\textsuperscript{c}Centre for Health Economics and Policy Analysis, McMaster University, 1280 Main Street West, Hamilton, ON, Canada, L8S 4K1

Abstract

This paper presents the results of a revealed-choice experiment testing the theoretical predictions of political economy models regarding public support for a publicly provided private good financed with proportional income taxes when individuals can purchase the good privately and either continue to consume public provision (‘top-up’) or forego public provision (‘opt-out’), but in each case continue to pay income taxes. Our laboratory results confirm behavior is consistent with the predicted majority-preferred tax rate under mixed financing with top-up, but we identify preferences for significantly higher rates of public provision than predicted under mixed financing with opt-out. Using non-parametric regression analysis, we explore the relationship between individuals’ top-up and opt-out decisions and both their income levels and the implemented tax rates.

Key Words: publicly provided private good, mixed financing, voting experiment

JEL: H42, H44, C91, D78

\textsuperscript{1}Corresponding Author: cuffk@mcmaster.ca, 905-525-9140 ext. 23827
1. Introduction

Mixed systems of public and private financing support the provision of many private goods such as education and health care. Unlike standard public goods, these goods are rivalrous in consumption and excludable. Systems of mixed finance of such private goods are characterized by regular (at times, seemingly endless) debate regarding the relative sizes and roles of the public and private sectors. Debate about the role of school vouchers in the education sector, public and private insurance in health systems internationally, and about public and private options for retirement savings typify policy discourse regarding mixed systems of finance. Debate often centers on the impact of alternative systems of mixed finance on choice, access, competition, quality, and, ultimately, on desired outcomes (e.g., student achievement, access to care, and income security). Formal economic analysis of mixed systems of finance for private goods emphasizes the potential impact of these systems on citizen support for public provision of the private good.

Analyses of the welfare effects of mixed systems of finance (e.g., Ireland 1990; Sonstelie, 1982; Marchand and Schroyen 2005) focus on the channels by which different configurations of public and private roles affect welfare. Central to the welfare effects is the income redistribution engendered by mixed systems of finance and its associated equity/efficiency trade-offs (e.g., Boadway et al. 1998; Besley and Coate 1991). These normative analyses highlight the crucial role that distributional issues play in the analysis of mixed systems of finance. Positive, political economy models that explicitly analyze how mixed finance affects public support for public provision typically assume that the degree of public funding is determined from majority-voting and the government is restricted from using a progressive linear income tax, so uniform provision of a

---

2Currie and Galvani (2008) provide a survey of the normative arguments for public provision of various private goods.
private good financed by a proportional tax is the only means to redistribute income in the economy. Such income redistribution receives support from a majority.\textsuperscript{3} As Glomm et al. (2011, p.617) note in the context of education, a key question of this literature is \textit{what is the majority preferred level of funding for tax-financed public education when private options are available?} A household’s private options typically include either that of ‘topping-up’ tax-financed public provision with private purchases (e.g., pay for private after-school tutoring lessons), or ‘opting-out’ of consuming the amount of public provision (e.g, send child to a private school instead of the local public school but continued to pay taxes to support the public school system).\textsuperscript{4} Internationally, one or both of these private options exist in many countries’ mixed financing systems for education, health care, and other private goods.

A key conclusion of this theoretical literature is that the type of private option available affects the majority-preferred level of public funding for the private good. If individuals can top-up public provision, induced preferences over public provision will be single-peaked and there exists a majority-rule equilibrium implementing the preferred policy of the median voter (Epple and Romano 1996a; Gouvieau 1997; Fernandez and Rogerson 2003). If instead individuals can opt-out of public provision then induced preferences are no longer single-peaked (Stiglitz 1974). A majority-rule equilibrium can, however, still exist (Glomm and Ravikumar 1998; Myers and L"ulfesmann 2011). If it does exist, then depending on the form of individual preferences the equilibrium will either be one in which the median voter is decisive or one in which there will be a coalition of high income and low income individuals against a coalition of middle-income individuals or ‘ends-against-the-middle’ (Epple and Romano, 1996b). A

\textsuperscript{3}Blomquist and Christiansen (1999) show that even with an unrestricted income tax, public provision of a private good will receive majority support since such provision enhances the efficiency of the income tax system given imperfect information about individuals' earning abilities.

\textsuperscript{4}A third option we do not consider in this paper is one in which individuals can opt-out of public provision and take their tax dollars with them.
common feature of all these models is that the tax-financed public provision of a private
good redistributes income from higher- to lower-income individuals.

Recent empirical literature has focused on two aspects of these majority-rule voting
models. First, papers have attempted to determine the effect of the income distribution,
in particular, income inequality, on the support for public spending on private goods.
(e.g. Corcoran and Evans 2010; Boustan et al. 2013). Second, papers have empirically
examined the nature of the political economy equilibrium, that is, whether the median
voter is decisive or whether there is an ‘ends-against-the middle’ outcome, for different
forms of public spending. For example, Cohen-Zada and Justman (2003) examines
public education spending, Kotakorpi and Laamanen (2010) looks at public health care
spending, and Brunner and Ross (2010) focuses on local public spending decisions.
And a recent paper by Bearse et al. (2013) calibrates a theoretical model similar to
the one we adopt under the status quo (a system of opting-out) to match U.S. data
and demonstrates that a uniform voucher system (similar to a system of topping-out)
will never receive majority-support. But, to our knowledge, no empirical studies have
directly tested the predictions of these models regarding the equilibrium level of the
public provision of the private good under alternative mixed systems of finance.

In this paper, we present the results of a series of controlled laboratory experiments
designed to test the theoretical prediction of a standard political economy model of
systems of mixed finance for a private good. We adopt a functional form for preferences
that ensures a majority-rule equilibrium exists for both the top-up and opt-out options
in an environment characterized by income heterogeneity and in which the median-
income individual is decisive. We consider three experimental treatments — public-
finance-only, mixed financing with top-up, and mixed financing with opt-out — and
examine their impact on the size of the tax-financed public system as determined by
majority-rule and on individual decisions about whether to exercise the private option
and to what extent, i.e., the quantity of their private purchases. We use a combination of within-subject and between-subject designs in which all subjects experienced ten decision periods of a public only financed treatment and ten decision periods of one of the two mixed financing systems (and we randomized the order of the public-only and mixed-finance treatments across experimental sessions to control for potential order effects).

Our aggregate analysis shows that the majority-preferred tax rate matched the predicted rate under public-only finance and mixed financing with top-up, but was significantly higher than predicted under mixed financing with opt-out. Counter to theoretical predictions, higher-income individuals support the public system in both types of mixed financing systems despite not having the financial incentive to do so. In contrast, lower-income individuals’ support for the public system is lower than predicted in both systems of mixed financing. Non-parametric regression analysis of individual-level decisions regarding whether to exercise the private option (top-up, opt-out) and the quantity of good to purchase privately found that under both forms of mixed financing, income level had a significant positive effect on the probability of exercising the private option, as predicted.

In the next section, we outline our political economy theoretical framework. In Section 3, we describe the laboratory implementation of the theoretical framework and present our experimental results in Section 4. Finally, we conclude in Section 5.

2. Theoretical Framework

The theoretical framework we adopt is based on standard majority-rule models of tax-financed public provision of a private good (see, e.g., Epple and Romano 1996a; Myers and Lülffesmann 2011; Bearse et al. 2013). Below, we outline the main features of these models and the specific functional form for household preferences that we use.
in each of the three treatments we consider (public finance only, mixed financing with a top-up option and with an opt-out option), and state the theoretical predictions.

2.1. Benchmark Model: Public Finance Only

There are \( N \) households who differ in their fixed income (or endowment of a numeraire consumption good) denoted by \( y \). The mean income in the population is \( \bar{y} \). The median income in the population, \( y_m \), is assumed to be less than the mean. Households have preferences over consumption of a numeraire good, given by \( c \), and of a specific private good \( E \) which may be publicly provided or purchased privately.\(^5\) To obtain closed-form solutions, we assume household preferences can be represented by the following utility function:

\[
U(c, E) = ac^\eta + bE^\eta
\]  

(1)

where \( a, b > 0 \) and \( \eta \in (0, 1) \). The private good \( E \) is produced using the numeraire good. Following the literature, it takes one unit of the numeraire good to produce one unit of the private good and this is independent of whether the good is publicly (i.e., tax-financed) or privately financed.\(^6\)

Consider first a public-only system where the provision of the private good is financed solely through a proportional income tax, whose rate is denoted by \( t \). This proportional tax rate is determined by majority-rule. The government provides a uniform amount of the private good to each household, denoted by \( g \).\(^7\) The government’s

\(^5\)For illustrative purposes, one could think of this private good as education, but the model can apply to any number of publicly provided private goods, such as garbage collection and health care. In the case of education, we can think about a household as comprising a parent and a child.

\(^6\)Following Glomm et al. (2011), one could interpret \( E \) as the quality of the private good being consumed. The production function for the quality of the good is linear in expenditure on the good regardless of which sector finances the good, i.e., publicly-financed or privately-financed.

\(^7\)For the remainder of the paper, we use the terms ‘public provision of the private good’ and ‘publicly financed private good’ interchangeably in referring to \( g \).
budget constraint is
\[ t\bar{y} = g. \tag{2} \]
Using the government’s budget constraint (2), the household’s budget constraint can be written as
\[ c = y - \left(\frac{y}{\bar{y}}\right)g \tag{3} \]
where \( T(y) = y/\bar{y} \) is the household’s relative tax price for the private good. Public provision of the private good effectively redistributes resources from households with incomes above the mean to households with incomes below the mean.

Substituting the household’s budget constraint (3) with \( E = g \) into (1), yields the household’s induced utility function over the public provision of the private good
\[ V(g) \equiv \max_{g \geq 0} a(y - T(y)g)^\eta + bg^\eta \tag{4} \]
which is strictly concave in \( g \). Therefore, each household has a unique preferred level of public provision of the private good, denoted by \( g(y) \), and a unique preferred tax rate, denoted by \( t(y) \), which are both strictly decreasing in household income. It follows directly from the median voter theorem that the equilibrium outcome under majority rule will be given by the preferred tax rate of the median income household, \( t(y_m) \), where
\[ t(y_m) = \frac{1}{\phi T(y_m)^{\frac{1}{1-\eta}} + 1} \tag{5} \]
and \( \phi = (a/b)^{\frac{1}{1-\eta}} \). The amount of publicly provided private good in equilibrium will be
\[ g(y_m) = \frac{y_m}{\phi T(y_m)^{\frac{1}{1-\eta}} + T(y_m)}. \tag{6} \]

**Theoretical Prediction 1** In a public-only financed system, preferred tax rates are strictly decreasing in income and the equilibrium outcome with majority-rule will be determined by the preferred tax rate of the median income household.
Next consider what happens to the equilibrium size of the public system when individuals can choose to supplement public provision of the private good with private purchases. We consider two cases: First, individuals can consume privately purchased amounts of the good in addition to the amount financed publicly (mixed financing with a top-up option) and second, individuals can substitute private consumption for the publicly financed private good, but must continue to pay taxes to finance public provision of the private good (mixed financing with an opt-out option.)

2.2. Mixed Financing with a Top-Up Option

Assume households can top-up public provision of the private good with individual purchases of the good. The timing of decision-making is as follows:

**Stage 1:** Households vote on a proportional income tax that finances the uniform provision of the private good, and the outcome is determined by majority rule.

**Stage 2:** Taking the amount of publicly provided private good as given, households choose how much additional amount of the good, denoted by \( s \geq 0 \), to purchase.

The solution is obtained by applying backward induction. At Stage 2, the household’s budget constraint is

\[
c = y - T(y)g - s
\]

and total consumption of the private good is \( E = g + s \). Therefore, the household solves the following problem in Stage 2:\(^8\)

\[
\max_{s \geq 0} a(y - T(y)g - s)^\eta + b(g + s)^\eta.
\]

Demand for the private good (as a function of \( g \)) by a household with income \( y \) is given

---

\(^8\)The second-order condition is satisfied.
by
\[ s(g) = \max\{h(y + (1 - T(y))g) - g, 0\}. \tag{9} \]

where \( h(y + (1 - T(y))g) \) is the demand for the good if the household had income \( y + (1 - T(y))g \).\(^9\) It follows from (9) that there is some level of publicly provided private good \( \hat{g}(y) \) above which a household with income \( y \) will not purchase the good where

\[ \hat{g}(y) = \frac{y}{\phi + T(y)}. \tag{10} \]

Next, consider the household’s induced preferences over the amount of publicly financed private good in Stage 1 which are given by

\[ W(g) \equiv \max_{g \geq 0} \ a(y - T(y)g - s(g))^{\eta} + b(g + s(g))^{\eta} \tag{11} \]

and are again strictly concave in \( g \).

Recall, households with income above the mean pay a higher price for \( g \) than for \( s \), that is, \( T(y) > 1 \) for \( y > \bar{y} \). Therefore, these households are better off with \( t = 0 \) \((g = 0)\) and purchasing all of the private good privately than with any positive tax rate. On the other hand, households with income below the mean pay a lower price for \( g \) than for \( s \), so such households are better off with a tax rate that ensures they do not top-up public provision at its optimum. Consequently, these households’ preferred tax rates are the same as in a public-only financed system. Given the median income is assumed to be below the mean, the equilibrium tax rate and public provision will be the same as in a public-only financed system and given by \( t(y_m) \) and \( g(y_m) \), respectively.

The decision to purchase the private good comes down to whether a household has some unmet demand for the good which can occur only if the household has sufficiently high (after-tax) income. A household will supplement the publicly provided private

\(^9\)The demand function \( h(\cdot) \) is obtained by maximizing (1) subject to \( c + s = y + (1 - T(y))g \).
good if $\hat{g}(y) \geq g(y_m)$ or using (10) and (6) if

$$y \geq y_m T(y_m)^{\frac{1}{n-1}} = \left(\frac{\bar{y}}{y_m}\right)^{\frac{1}{1-\eta}} y_m.$$ (12)

A necessary condition for (12) to be satisfied is that the household has an income above the mean income. Further, since $\hat{g}(y)$ is increasing in income it follows that for the set of incomes such that (12) is satisfied, private purchases will be increasing in income.

**Theoretical Prediction 2** In a mixed financing system with a top-up option, households with incomes greater than the mean prefer a zero tax rate. All other households prefer the same tax rates as in a public-only financed system. The size of the public system will be the same as in a public-only financed system. Households with sufficiently high income will top-up the public provision of the private good with private purchases and the amount of private purchases will be increasing in income.

2.3. Mixed Financing with an Opt-Out Option

Now assume that households can privately finance their consumption of the private good, but only if the household opts-out of consuming the publicly provided private good and continues to pay taxes to finance public provision of the private good. In this financing scenario, the amount of the publicly provided private good available to a given household will depend on the number of households who opt-out. Let $N^*$ be the number of households who consume the publicly provided private good, so $N - N^*$ is the number of households who choose to opt-out. The amount of publicly provided private good per capita will be

$$g = t \frac{N}{N^*} \bar{y}.$$ (13)

The timing of decision-making is as follows:

**Stage 1:** Households vote on a proportional income tax that finances the uniform provision of the private good to those households who do not opt-out of consuming
the publicly financed private good and the outcome is determined by majority rule.

**Stage 2:** Taking as given both the amount of public provision of the private good and the opt-out decisions of other households, each household chooses whether to consume the amount of publicly provided private good or to opt-out and purchase all of their consumption of the good privately.

Using backwards induction, consider first a household who chooses to opt-out. This household solves the following problem

\[
\max_e a(y(1-t) - e)^\eta + be^\eta
\]

where \(e\) is private expenditure on the private good which yields the demand \(h(y(1-t)) = y(1-t)/(\phi + 1)\). Substituting this demand back into the household’s objective yields the household’s maximized level of utility if the household opts out (given \(t\))

\[
\left[\frac{y(1-t)}{\phi + 1}\right]^\eta \left[a\phi^\eta + b\right]
\]

which is increasing in income. A household who does not opt-out has utility

\[
a(y(1-t))^\eta + b \left(t \frac{N}{N^* y}\right)^\eta
\]

which is also increasing in income, but at a slower rate than (15). Therefore, a household with an income greater than \(\hat{y}(t,N^*)\) will optimally choose to opt-out and households with income below \(\hat{y}(t,N^*)\) will optimally consume the amount of public provision of the private good, where by equating (15) and (16),

\[
\hat{y}(t,N^*) = K \left(\frac{t}{1 - t N^* y}\right)
\]

\[10^\text{This follows from assuming that } [{\phi^\eta + b/a}/(\phi + 1)]^\eta > 1.\]
and $K > 0$.\(^{11}\) This cut-off income level is increasing in $t$ and decreasing in $N^*$ as one would expect.\(^{12}\)

In equilibrium, the number of individuals choosing not to opt-out given the equilibrium tax rate, i.e., those with incomes less than $\hat{y}(N^*, t)$, must be exactly equal to $N^*$. This condition determines $N^*$ as a function of $t$. Suppose income is distributed according to the cumulative distribution function $F(y)$ with a corresponding density $f(y) > 0$ for all $y$, then the condition implicitly determining $N^*(t)$ is $N^* = F(\hat{y}(N^*, t))$ where $N^*(t) > 0$.

By comparing (15) and (16) given $N^*(t)$, under the opt-out option, for $t$ close to zero households with any income prefer a private-only financed system, and for $t$ close to 1 households with any income prefer a public-only financed system. Therefore, as shown in Myers and Lülfesmann (2011), there must exist some critical tax $\hat{\tau}(y)$ between (0,1) such that a household with income $y$ is indifferent between opting-out or not (treating $N^*$ as a function of $t$) in Stage 2. For tax rates higher than $\hat{\tau}(y)$, the household is better off not opting-out and for tax rates lower than $\hat{\tau}(y)$, the household is better off opting-out. This critical tax rate is increasing in income. One way to interpret this result is that higher income households are better off opting-out over a larger range of tax rates than lower income households.

Consider Stage 1. For households who opt-out in Stage 2, their preferred tax rate is zero regardless of the opt-out decisions of other households since these households continue to pay taxes to finance the public provision of the private good, but do not consume any of the publicly financed private good. A household that does not opt-out

\(^{11}\)That is, $K = \frac{(b/a)^{1/\eta}}{[[\phi]\eta^{\phi+b/a}-1]^{1/\eta}} > 0$.

\(^{12}\)We have $\partial \hat{y}/\partial t = \hat{y}/[t(1-t)^2] > 0$ and $\partial \hat{y}/\partial N^* = -\hat{y}/N^* < 0$. 

12
solves the following problem:

$$\max_{t \in (0,1)} a(y(1-t))^{\eta} + b \left( \frac{N}{N^*(t) \widehat{y}} \right)^{\eta}$$

where the household treats $N^*$ as a function of the tax rate. Define the solution as $t^*(y)$ where $t^*(y)$ will be decreasing in income.

Consider the median income household. Suppose $\hat{t}(y_m) < t^*(y_m)$. Then the median income household will choose to vote for $t^*(y_m)$ since they obtain higher utility by not opting-out. In this case, since $\hat{t}(y)$ is increasing in income and $t^*(y)$ is decreasing in income, higher income households will vote for a lower tax rate, possibly zero, and lower income individuals will vote for a tax rate higher than $t^*(y_m)$. Therefore, $t^*(y_m)$ will be the equilibrium tax rate. If instead $\hat{t}(y_m) > t^*(y_m)$, the median income household will vote for a zero tax rate and opt-out, and the equilibrium tax rate will be zero. In this case, all individuals will opt-out by default.

**Theoretical Prediction 3** In a mixed financing system with an opt-out option, the outcome is again determined by the median income household’s preferred tax rate. If the median income household has a positive preferred tax rate, then all lower income households will not opt-out of the public system and preferred tax rates will be decreasing in income. Only households with sufficiently high income will opt-out of the public system and will have a preferred tax rate of zero.

3. Laboratory Implementation

The purpose of the experiment is to test the above theoretical predictions of majority-rule voting over the tax-financed public provision of a private good under public-only financing, mixed financing with a top-up option and mixed financing with an opt-out option. Following standard experimental economic methodology, subjects in the experiment are incentivized with real monetary payoffs and the experiment is
framed in a neutral context to minimize potential content-related framing effects (Alm and Jacobson 2007). Subject decisions are framed as choices over how much to invest in alternative investment funds, including a collective fund and an individual private fund.\(^{13}\) The complete set of instructions used in the experiment can be found in Appendix B.

The experiment used a combination of within-subject and between-subject designs. All subjects experienced ten decision periods of a public only financing treatment and ten decision periods of one of the two mixed financing systems, where the order of the two treatments (public/mixed) was randomized across the different experimental sessions to control for potential order effects. Comparison of the baseline public-only financed system and the two mixed financing systems relies on within-subject variation, while the comparison of the different mixed financing systems (top-up and opt-out) relies on between-subject variation. In the public-only decision periods individuals were assigned an exogenous income of laboratory dollars and asked to choose their preferred proportional tax rate knowing that the median tax rate submitted would determine the tax rate for the period. In each mixed financing decision period individuals were assigned an exogenous income of laboratory dollars and asked to make two sequential decisions. First, individuals were asked to choose a proportional tax rate and second, individuals were asked how much of the good to purchase privately given their income, the tax rate (as determined in the first stage) and the treatment (top-up, opt-out). Finally payoffs were realized.

Each session ran with ten subjects each of whom was told that they would be randomly assigned to be a member of a group of five people, but were not told who else was in their group. Each group remained together through the session (following

\(^{13}\)Compared to framing decisions in the context of education or health care, the current neutral framing might bias findings against public provision of these private goods.
Kroll et al., 2007 and Margrieter et al., 2005) so that the two groups in each session represented independent observations. Subjects were told that, at the beginning of each decision round, each member of their group would randomly be assigned an income, expressed in laboratory dollars (L$), from the following set of five income levels (125, 275, 640, 700, 1500), and that each individual would be assigned each of the income levels twice over the course of the session. The income distribution was chosen to ensure that the median income was below the mean (consistent with the theoretical assumption). To keep subjects actively thinking about their decisions, incomes were assigned in a pre-determined pseudo-random order such that subjects experienced each of the five income levels in the first five periods of each treatment and then again in the last five periods of each treatment, but in a different order.

Twenty groups of five subjects were recruited using an online recruitment system for controlled laboratory experiments (ORSEE, Greiner 2003) and the experiment was administered in the McMaster Experimental Economics Laboratory. Five groups each experienced the following ordering of treatments: public-only followed by top-up; top-up followed by public-only; public-only followed by opt-out; and opt-out followed by public-only. Each experimental session had twenty decision periods (ten decision periods for each treatment) and lasted approximately 70 minutes. The average subject payoff was $23 including a $5 show-up fee. Subjects were individually paid their cash earnings in private. The experiment was conducted using z-Tree software (Fischbacher 2007) and the laboratory protocol was approved by the McMaster University Research Ethics Board. Observations from the 100 subjects are included in the results below.

3.1. Publicly Financed Provision of the Private Good

At the beginning of each decision period of the public-only finance treatment, subjects were told that their income must be divided between two Investment Funds: a Group Investment Fund (GIF) and a Private Investment Fund (PIF). Subjects were
told that everyone in their group must contribute the same fixed percentage of their income to the GIF and that this percentage would be determined by the group. The total amount contributed to the GIF would be divided into five equal shares. Each share would be invested in Market A and the subject would earn a return from this investment. The subject’s remaining income after contributing to the GIF would go into the subject’s PIF and invested in Market B where it would earn a return for the subject.

The returns earned on the investments were calculated using the payoff function given by (1), where the GIF investment in Market A is for the private good $E$ and the PIF investment in Market B is for the numeraire good $c$ with the following parameter values: $a = 20$, $b = 22$ and $\eta = 0.6$. This parameter set was chosen to ensure salience in the payoffs and to obtain theoretical predictions of some topping-up and opting-out in equilibrium.

In each of the decision periods of the public-only treatment, subjects were asked to submit their preferred mandatory GIF contribution rate. To replicate the outcome of majority-rule in a laboratory environment, subjects were told that submitted GIF contribution rates would be ranked from highest to lowest and that the median contribution rate would be implemented.\footnote{Differing voting processes have been implemented experimentally. The seminal work by Fiorino and Plott (1978) uses a sequential amendment driven voting protocol while more recent papers use either simultaneous voting protocols (e.g., Margreiter et al. 2005; Kroll et al. 2007) or a binary yes/no vote on a given tax proposal (e.g. Sutter and Weck-Hannemann 2003.) Another approach is to allow each individual to propose a tax rate and to implement the median tax rate (e.g. Norton and Isaac 2013.) We adopt the latter voting process since it most closely resembles the theoretical environments that were being implemented in the lab.} It was explained to them why there was no incentive to submit a contribution rate other than their preferred rate.

Subjects were provided with a table to illustrate how their returns worked in the markets. Subjects were also given a tutorial with examples to ensure their comprehension about how payoffs are determined in the treatment. The tutorial explained to
subjects how they could use the onscreen calculator to determine both their returns in each market and their total payoff for different GIF contribution rates. The calculator removed the complexity of the payoff function and explicitly allowed subjects to calculate the payoffs earned by themselves and others in their group with different incomes. Subjects were able to access the calculator throughout the session.

3.2. Publicly Financed Provision of the Private Good with a Top-up Option

In the top-up treatment, subjects were provided the same information as in the public-only treatment (described above), but were also told that they could choose to invest some of their PIF contribution in Market A rather than having it all automatically invested in Market B (Market A represented the private good that was being publicly funded). This additional investment decision could only be made, however, after the mandatory GIF contribution rate had been determined. Subjects were therefore first asked to submit their preferred GIF contribution rate, told the resulting GIF contribution rate that was to be implemented, and then asked how much of their PIF they would like to invest in Market A to supplement their GIF contribution. Any income remaining was automatically invested in Market B. Before submitting their preferred GIF contribution rate and before deciding how much to invest in Market A, individuals were again provided with an online calculator that allowed them to calculate their total return for different income levels, GIF contribution rates and individual PIF investments in Market A.

3.3. Publicly Financed Provision of the Private Good with an Opt-out Option

In the opt-out treatment, subjects were also provided with the same information as in the public-only treatment, but were also told that they could choose to invest some of their PIF in a third market, Market C. Investments in Market C would earn the same returns as in Market A. This private investment decision could only be made after the mandatory GIF contribution rate had been determined but, unlike the top-up
treatment, if the subject choose to make a private investment in Market C then they would no longer receive a share of the GIF. The total GIF was divided equally only among those members of the group who did not invest in Market C. These subjects would, however, still have to make the mandatory contribution to the GIF. As in the other two treatments, before deciding on what GIF contribution rate to submit and how much to invest in market C, subjects were provided with an online calculator that allowed them to calculate their total return for different income levels, GIF contribution rates, number of others investing in Market C, and individual PIF investments in Market C.\footnote{For all three treatments, at the end of each decision period individuals were provided with summary information on the implemented GIF rate and the subjects’ investment decisions, including the returns to the different investment decisions and the subject’s final payoff.}

Table 1 shows the theoretically predicted tax rates (i.e., mandatory GIF contribution rates) for the three treatments and Table 2 shows the theoretical predictions for the preferred tax rates by income for the three treatments.\footnote{Numerical predictions for the three treatments were obtained by applying the theoretical results to the discrete income distribution used in the experiment.}

4. Experimental Results

We begin by testing for both order and learning effects with respect to the variables of interest; the mean implemented GIF rate (hereafter referred to as the “the tax rate”)\footnote{Implemented GIF rate refers to the median contribution rate and is used to calculate subject payoffs at the end of a given decision period.}, the mean top-up/opt-out frequencies and the mean private purchases conditional on topping-up/opting-out. Our tests confirm an absence of order effects, so for the remainder of our analysis we pool the data across the two possible orderings of treatments (public-only treatment followed by one of the mixed financing treatments and one of the mixed financing treatments followed by the public-only treatment).\footnote{Because the ordering of treatments was varied between subjects, the mean observations are independent; we therefore test for order effects using both Mann-Whitney and Fisher-Pitman Randomiza-}
Our tests also confirm an absence of any learning effects for all of the variables of interest except for the mean frequency of opting-out and the corresponding mean private purchases conditional on opting-out.\textsuperscript{19} Given this evidence of some learning effects, we only use data from the last five decision periods for all treatments in our analysis.

We examine the following outcomes: the implemented and submitted, or preferred, tax rates in the three treatments, the decision to top-up and and how much to purchase privately if topped-up, and the decision to opt-out and how much to purchase privately if opted-out. Each treatment includes ten independent observations for between-group comparisons. For tests of differences between public-only and top-up or opt-out treatments the unit of observation is the mean observed values of the difference between focus variables over the last 5 decision periods for each 5-person group in each treatment. There are ten independent observations for each difference between treatments for within-group comparisons. The descriptive analysis uses both nonparametric Mann-Whitney or Wilcoxon signed-rank tests and parametric unpaired or paired t-tests, as appropriate. Due to the small sample sizes significant differences from null hypotheses are judged at a 10\% critical value.

4.1. Observed Tax Rates
4.1.1. Mean Implemented Tax Rates

The observed mean implemented tax rate for each of the public-finance-only and top-up treatments does not differ from the theoretically predicted rate of 56.39 (Table 1).\textsuperscript{20} Only in the opt-out treatment is the mean observed implemented rate...
(54.58) statistically different from its predicted rate (26.51). The mean implemented tax rates do not differ between each of the three treatments.

4.1.2. Mean Preferred Tax Rates by Income

Table 2 presents the observed mean preferred tax rates and the theoretically predicted values by income. Recall, all subjects experienced each of the five different income levels. For the public-only treatment the mean observed preferred tax rates are decreasing in income as predicted, and only for the lowest income level (125) are the mean observed preferred rates statistically different from the predicted rate by meaningful amounts (e.g., 86.36 and 86.10 vs. 93.70). Interestingly, in this case, the observed preferred tax rate is less than the predicted preferred rate.

For the top-up treatment, the observed mean tax rates of the two lowest income levels are less than predicted by theory and the mean preferred tax rates of the two highest income levels are notably higher than the predicted rates of zero. The mean preferred tax rate of the median income level, however, is not statistically different from the predicted rate and consequently, as discussed above, the mean implemented tax rate did not differ from the predicted rate. Except for income level 700, the preferred tax rates under top-up do not differ significantly from those under public-finance-only.

For the opt-out treatment, the observed mean preferred tax rates are significantly less than the predicted levels for the two lowest income levels and significantly higher than the predicted levels for the two highest income levels. In this treatment, the mean preferred tax rate of the median income level (54.94) is also significantly higher than

---

21 The intuition for the lower tax rate in opt-out compared to top-up (26.51 vs. 56.39) is that, under opt-out, if the median voter raised her preferred tax rate then the highest income individual would no longer choose to opt-out and the median voter would be worse off than with a higher tax rate since the total amount of public provision would now be shared among a greater number of people.
the predicted rate of 26.5. The mean preferred tax rates in the opt-out treatment are significantly lower than in the public-finance-only treatment for the two lowest income levels.

4.2. Decision to Top-up and By How Much

The mean implemented tax rate in the top-up treatment did not differ statistically from the predicted rate. Therefore, we would expect the average top-up behavior of subjects to match the predictions. With our assumed payoff function and parameter values, individuals with the two highest income levels, L$700 and L$1500, are predicted to make private purchases of the amounts L$9.71 and L$204.84 (Table 3) at the predicted equilibrium tax rate. In the experiment the highest income subjects topped-up most (78%) of the time and, among those high-income subjects who topped up, the average top-up amount was a little more than the amount predicted (L$269.41 versus L$204.84). For the second-highest income, subjects topped-up just over half of the time (60%) and the mean amount of top-up among those who chose to top-up was L$77.33 which exceeded the predicted amount of L$9.71. Even though they were predicted not to top-up at the equilibrium predicted tax rate, median income subjects exhibited similar behavior to those with the second highest income, topping-up about half of the time (56%) and, among those who chose to top-up, topping-up on average L$71.86. Subjects with the two lowest-income chose to top-up 24% and 22% of the time and, among those subjects who chose to top-up, topped-up on average L$35.04 and L$65.11, respectively, even though they too were predicted not to top-up at the predicted equilibrium tax rate.

As just described, the average frequencies of top-ups and amounts of top-up per person conditional on topping-up differed from their predicted values (Table 3). In interpreting these results, it needs to be kept in mind that although the mean observed tax rate did not differ from the predicted tax rate, the tax rate individual subjects
actually faced when deciding whether and by how much to top-up could have differed substantially from the mean observed tax rate so deviations from the predictions in Table 3 are not necessarily sub-optimal for individual subjects. To uncover the relationship between the actual implemented tax rate the subject faced and their decisions to both top-up and by how much to top-up by, we use nonparametric local linear regression.\textsuperscript{22}

Although this technique does not explicitly model correlations in subject decisions across periods that could potentially reduce the significance of the implemented tax rate and of the income level in predicting individual decisions, our experimental design mitigates the possibility of such correlation for two reasons. First, the experimental design reassigns income to subjects after each decision period and so subjects do not benefit from reporting the same preferred tax rate each decision period. Second, because the median reported preferred tax rate becomes the implemented tax rate in each decision period, subjects have an incentive to reveal their true preferred tax rate, which is related to their period-specific assigned income.

Using R’s (R Core Team, 2012) \textit{np} package from Hayfield and Racine (2008) for nonparametric local-linear regression, we obtain a 3-dimensional object defined on the following three axes: 1) the predicted probability of topping up, 2) the implemented tax rates resulting from the experiment and 3) the five income levels. Interactions are automatically incorporated since all dimensions are estimated simultaneously.\textsuperscript{23}

\textsuperscript{22}This approach does not have any prior hypotheses about their specific functional forms and relies only on the assumptions that the joint distribution exists, is differentiable and its second moment is finite. This approach avoids imposing a mis-specified parametric model while nesting the parametric linear model. See Li and Racine (2004) for further details. The non-parametric estimator uses a product kernel consisting of an Epanechnikov kernel for the continuous implemented tax rate and a Wang and Van Ryzin kernel for the ordered income levels. Bandwidths were chosen using the data-driven improved Akaike Information criterion (Hurvich, Simonoff and Tsai 1998.) Error bounds were calculated by bootstrapping the entire fitted object (with 399 replications.) Nonparametric significance testing was undertaken following Hayfield and Racine’s (2008) \textit{np} package which is analogous to the parametric t-test and also employs bootstrapping.

\textsuperscript{23}Experimental session group is not included in the following analysis. Including it as a factor variable in the local linear regression was found to be insignificant except for the probability of topping up. In this case, the effect was not attributable to differences in behavior across groups within income classes.
Viewing one plane of the object with the implemented tax rates as the \( x \) axis and predicted probabilities of topping up as the \( y \) axis yields Figure 1. Figure 2 illustrates similar results for the predicted amounts of topping-up.

4.2.1. Nonparametric Analysis: Decision to top-up

By disaggregating the session-level data, we can determine whether income explains individual subjects’ top-up behavior and how the actual implemented tax rate affected a subject’s top-up decision. The non-parametric analysis reveals that the probability of topping up is significantly affected by both the implemented tax rate and income level (\( p = 0.0075 \) and \( p = 0.0000 \) respectively) as shown in Figure 1. At low tax rates (around 40%, below which 12.5% of the observations fall), the probability of topping up ranges from about 0.43 for people with incomes of 125 to 0.90 for people with incomes greater than 275. At high tax rates (around 75%, above which about 12.5% of the observations fall), the probability of topping up narrows across incomes to about 0.07 for incomes of 125 to between 0.11 and 0.37 for people with incomes of 275, 640 and 700 and .52 for people with incomes of 1500.

Figure 1 also shows a significant non-linear relationship between the probability of topping up and income.\(^24\) Between tax rates of 20% and 55% the probability of topping up is significantly less for those with incomes of 125 and 275 than for those with incomes of 640, 700 and 1500. For tax rates between 55% and 75% the probability of topping up is higher for those with an income of 1500 than it is for the four other incomes. The probabilities of those with the middle incomes of 640 and 700 switches at tax rates between 50% and 60%: at rates less than 50%, they have high probabilities of topping

\(^{24}\)The nonparametric approach provides the needed flexibility to identify these highly non-linear relationships. The coefficient of determination for the nonparametric model is 0.41, versus 0.29 for a parametric probit model.
up and their behavior tracks that of those with incomes of 1500; but just as the tax rate reaches 50%, their probability of topping up falls precipitously, and above rates of 60%, they have relatively low probabilities of topping up and their behavior tracks closely that of those with incomes of 125 and 275.

4.2.2. Nonparametric Analysis: Private purchases given topping-up

The nonparametric analysis of the amount of private purchases conditional on choosing to top-up finds that such purchases are also significantly affected by both the implemented tax rate and by income (p = 0.0000 and p = 0.0000 respectively). The significant effect of income is reflected in Figure 2 by the gap between the confidence bands for the individuals with incomes of 1500 and the confidence bands of the individuals with incomes between 700 and 125. The significant effect of the implemented tax rate is reflected by the absence of overlap of the confidence bands at low tax rates when compared with the confidence bands at high tax rates for the income level 1500 (e.g., compare the band at the tax rate at the 12.5th percentile with the band at the tax rate of 87.5th percentile relative to the bands at the 25th percentile and 75th percentile). The amount of private purchases by subjects choosing to top-up at low tax rates is significantly higher than the amount of private purchases by subjects choosing to top-up at high tax rates. This finding is intuitive and consistent with the theory.

4.3. Decision to Opt-out and How Much to Purchase Privately

Only the highest income individual was predicted to opt-out at the predicted equilibrium tax rate, and this individual was predicted to make private purchases of L$616.53 (Table 3). The observed mean implemented tax rate under opt-out was significantly higher than the predicted rate of 26.51%, a difference important for trying to understand the observed opt-out decisions. The highest income household should opt-out only if the realized tax rate is less than or equal to 28.9% which was true only 8% of the
The mean observed frequency of opt-outs for the highest income individual was 20%, significantly lower than the predicted rate of 100% and significantly higher than the prediction of 8% conditional on realized tax rates. For the 125, 640 and 700 income levels, observed frequencies of opt-outs are significantly higher than the prediction of zero (although deviations are small, 6%, 6% and 10%, respectively).

The highest income individuals who opted-out had an observed average private purchase amount of L$562.5 which is not significantly different from the predicted amount of L$616.53. For four of the income levels, the average amounts of private purchases per person when opting out are not significantly different from the predicted amount of zero. The only amount that is significantly different from the prediction is for individuals with income of 700, who purchased L$187 on average, significantly more predicted. But, as mentioned the observed mean implemented tax rate differed significantly from the predicted rate and therefore, to better understand the relationship between the actual implemented tax rate and both the likelihood of opting out and the amount an individual privately purchases conditional on opting-out, we use a nonparametric local linear regression.

4.3.1. Nonparametric Analysis: Decision to opt-out

Nonparametric local linear regression indicates that the probability of opting out of the publicly provided private good is significantly affected by both the actual implemented tax rate and income (p = 0.0000 and p = 0.0450 respectively). The relationship between the probability of opting out and the implemented tax rate is clearly shown in Figure 3 by income level. At low tax rates (below 30%, which includes about 12.5% of the observations), the probability of opting out ranges from about 0.10 for people with incomes of 125 to more than 0.30 for people with incomes of 1500. At high tax rates of 28.9%, the household is indifferent between opting-out or not. At any higher tax rate, the highest income household is strictly better off not opting-out.
rates (above 80%, which also includes about 12.5% of the observed rates), the probability of opting out narrows across incomes to less than 0.10 for all levels of income. The significant relationship between the probability of opting out and income level is difficult to see from Figure 3. But, for more than 60% of the observations (between implemented tax rates of about 30% and about 70%) the 90% confidence bands do not overlap between the highest income participants, with income of 1500, and those with the lower incomes of 125 and 275. There is substantial overlap of the confidence bands around the top three income levels (1500, 700 and 640) over most tax rates and around the bottom four income levels (125, 275, 640 and 700).

4.3.2. Nonparametric Analysis: Private purchases given opting-out

The amount of private purchases conditional on choosing to out-out is not significantly affected by the actual implemented tax rate, but is significantly affected by the income level ($p = 0.2456$ and $p = 0.0025$ respectively). The significant effect of income is reflected in Figure 4 by the gap between the confidence bands for the individuals with incomes of 1500 and the confidence bands of the individuals with income between 700 and 125. The insignificant effect of the tax rate is reflected by the overlap of the confidence bands though the entire range of tax rates for each income level.

5. Conclusion

This laboratory experiment represents the first empirical test of theoretical predictions regarding support for the public provision of a private good, such as education, under alternative mixed financing system. We found that subject behavior was generally consistent with the theoretical predictions of a mixed system of finance with top-up and of a pure publicly financed system, but we identified an important treatment effect of a mixed system of finance with opt-out. Under mixed financing with opt-out, subject behavior lead to an outcome with significantly higher public provision of the private
good than was predicted by theory. On the whole, subjects exhibited the expected income-gradient with respect to preferred tax rates — high-income subjects preferred lower tax rates than did low-income subjects. Further, the individual-level analysis revealed that, under both mixed financing systems, when choosing whether and by how much to exercise the private-purchase option subjects responded as predicted to variation in their income and in the tax rate they faced.

The public provision of a private good such as education is often motivated by an equity concern, a desire to reduce inequality in consumption of the good. Pure public provision ensures that an equal amount of a good is provided to everyone. But public provision with private top-up or opt-out may achieve equity objectives without completely removing the opportunity for private purchases. An important question is the extent to which allowing private purchases under mixed financing affects inequality in consumption and payoffs to subjects (given by equation 1), where in our environment total payoffs provide a measure of social welfare. Using the coefficient of variation (CoV) as a convenient measure of inequality\(^{26}\), in our environment a public-only system of financing is predicted to have perfect equality in consumption (CoV = 0) and a CoV of 0.22 for payoffs, mixed financing with top-up is predicted to result in CoVs of 0.22 and 0.23 for consumption and payoffs respectively, and mixed financing with opt-out is predicted to result in CoVs of 0.61 and 0.29 for consumption and payoffs.\(^{27}\) Allowing private purchases through top-up, therefore, is predicted to still redistribute income and achieve equity improvements on par with those under public-only finance. Opt-out is predicted to produce similar equity in payoffs as public-only finance, but to have notably greater inequality in consumption of the private good.

---

\(^{26}\)In our setting the CoV equals 0 when there is perfect equality in consumption/payoffs and would equal 2.3 if one individual had all of the income, so the other four individuals had zero payoffs.

\(^{27}\)Predicted and observed CoVs are provided in Tables A.3 and A.4 of Appendix A and have been calculated using the information in Tables A.1 and A.2, respectively.
Focusing first on consumption, by the very nature of the public-only treatment the mean observed CoV for consumption is, as predicted, equal to 0. Under top-up, the mean observed CoV of 0.24 is not significantly different from the predicted value of 0.22. The results under opt-out, however deviate from predictions: the distribution of consumption is significantly more equal than predicted (CoV of 0.15 versus the prediction of 0.61). Consumption under opt-out is distributed more equally than predicted because the implemented tax rate was significantly higher than predicted and therefore, low-income individuals consumed more of the good (though public provision) than predicted and high-income individuals consumed less (because of lower-than-predicted private purchases).

Observed distributions of payoffs corresponded to predictions for both public-only and top-up financing, but the distribution of payoffs under opt-out is more equal than predicted (0.24 vs. 0.29). Inequality in the observed distributions of payoffs do not differ meaningfully between the three systems of finance (CoVs of 0.24 for both top-up and opt-out; CoV of 0.22 for public-only when matched with top-up and 0.23 when matched with opt-out). A comparison of observed mean total payoffs reveals that the differences are all small (less than 2%) both against predictions and across the different treatments. Overall, these distributional results reflect the subjects’ behavior across the three treatments.

The experiments reported here provide a baseline set of controlled laboratory results and leave for future work the testing of more complicated models that consider alternative behavioral hypotheses and different political mechanisms. For example, several recent experimental papers have investigated majority-voting over redistribution and focus on the role of inequality aversion or fairness considerations (Höchtl et al. 2012; Ackert et al 2007), social identity (Klor and Shayo 2010), and source of income, i.e., endowed or task-based (Balafoutas et al. 2013), in explaining preferences for redistribution.
as expressed through the voting mechanism. Testing for preferences over redistribution will require modifying the underlying behavioral model to obtain predictions consistent with various characterizations of people who have other-regarding preferences.\footnote{Work by Clark (1998), Tyran and Sausgruber (2006), Ackert et al. (2007), Klor and Shayo (2010), Messer et al. (2010) and Höchtl et al. (2012) indicate that other-regarding preferences can be important in laboratory contexts.}

Only recently has other-regarding preferences been integrated into theoretical political economy models (e.g., Dhami and Al-Nowaihi 2010).

Second, people generally express preferences of the provision of services rather than tax rates. For instance, a more “realistic” approach to collective decision-making through majority-rule voting might be to have participants vote of levels of spending rather than taxes. Alternatively, actual tax rates typically result from a process that is not a direct part of the public referendum process. For example, Fréchette et al. (2012) and Battaglini et al. (2012) present laboratory environments in which public good provision is presented within the context of legislative bargaining. Subjects might find this quite different frame a more natural way to think about the problem.
Table 1: Predicted and Implemented Tax Rates by Treatment, Last 5 Periods

<table>
<thead>
<tr>
<th></th>
<th>Top-Up Sessions</th>
<th></th>
<th>Opt-Out Sessions</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Public-Only</td>
<td>Top-Up</td>
<td>Public-Only</td>
<td>Opt-Out</td>
</tr>
<tr>
<td>Predicted Tax Rate</td>
<td>56.39</td>
<td>56.39</td>
<td>56.39</td>
<td>26.51</td>
</tr>
<tr>
<td>Observed Mean</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Implemented Tax Rate</td>
<td>58.38</td>
<td>54.24</td>
<td>55.24</td>
<td>54.58*</td>
</tr>
<tr>
<td>(Standard Deviations)</td>
<td>(4.68)</td>
<td>(11.61)</td>
<td>(3.53)</td>
<td>(11.13)</td>
</tr>
<tr>
<td>Observations</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>

Notes: Statistically significant differences between an observed value and those from other treatments or between an observed value and its predicted value are indicated with superscripts. All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value.
Table 2: Predicted and Observed Tax Rates by Income and Treatment, Last 5 Periods

<table>
<thead>
<tr>
<th>Income</th>
<th>Predicted Preferred Rate</th>
<th>Top-Up Sessions</th>
<th>Opt-Out Sessions</th>
<th>Observed Preferred Rate</th>
<th>Observed Preferred Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>125</td>
<td>93.7 93.7 93.7</td>
<td>86.36* 83.60*</td>
<td>86.10^O^* 75.94^P^*</td>
<td></td>
<td></td>
</tr>
<tr>
<td>275</td>
<td>82.1 82.1 82.1</td>
<td>79.86 73.98*</td>
<td>78.34^O^ 68.22^P^*</td>
<td></td>
<td></td>
</tr>
<tr>
<td>640</td>
<td>56.4 56.4 26.5</td>
<td>56.56 52.36</td>
<td>51.94* 54.94*</td>
<td></td>
<td></td>
</tr>
<tr>
<td>700</td>
<td>53.1 0 0</td>
<td>53.30^T^ 42.22^P^*</td>
<td>49.62* 50.22*</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1500</td>
<td>26.5 0 0</td>
<td>25.72 29.10*</td>
<td>25.84 29.16*</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value. ^T^ indicates that there is a statistically significant difference between the top-up or opt-out value and associated public value. ^O^T^ indicates that there is a statistically significant difference between the observed opt-out (top-up) value for the treatment to which the superscript is attached.
### Table 3: Predicted and Observed Private Investments in Market A (Top-Up) or Market C (Opt-Out), Last 5 Periods

<table>
<thead>
<tr>
<th>Income</th>
<th>Predicted Investment in Market A (Top-up)</th>
<th>Observed % who Top-up</th>
<th>Observed Mean Investment in Market A (Top-up)</th>
<th>Predicted Investment in Market C (Opt-out)</th>
<th>Observed % who Opt-out</th>
<th>Observed Mean Investment in Market C (Opt-out)</th>
</tr>
</thead>
<tbody>
<tr>
<td>125</td>
<td>0</td>
<td>24%*</td>
<td>35.04*</td>
<td>0</td>
<td>6%*</td>
<td>22.33</td>
</tr>
<tr>
<td>275</td>
<td>0</td>
<td>22%*</td>
<td>65.11*</td>
<td>0</td>
<td>0%</td>
<td>0</td>
</tr>
<tr>
<td>640</td>
<td>0</td>
<td>56%*</td>
<td>71.86*</td>
<td>0</td>
<td>6%*</td>
<td>140.66</td>
</tr>
<tr>
<td>700</td>
<td>9.71</td>
<td>60%*</td>
<td>77.33*</td>
<td>0</td>
<td>10%*</td>
<td>186.80*</td>
</tr>
<tr>
<td>1500</td>
<td>204.84</td>
<td>78%*</td>
<td>269.41*</td>
<td>616.53</td>
<td>20%*</td>
<td>562.5</td>
</tr>
</tbody>
</table>

Notes: Investments are in L$ per subject. A predicted investment amount of 0 implies that the individual is not predicted to top-up or opt-out. All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value.
Figure 1: Probability of Topping Up by Income and Implemented Tax Rate
Figure 2: Amount Topped Up by Income and Implemented Tax Rate
Figure 3: Probability of Opting Out by Income and Implemented Tax Rate
Figure 4: Amount Opted Out by Income and Implemented Tax Rate


rics: The np package,’ Journal of Statistical Software 27(5). URL: http://www.jstatsoft.org/v27/i05/


Appendix A. Additional Tables
Table A.1: Per Period Consumption of Private Good by Treatment and Income, Last 5 Periods

<table>
<thead>
<tr>
<th>Income</th>
<th>Sessions with Top-Up</th>
<th>Sessions with Opt-Out</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Public only Predicted</td>
<td>Top-Up Predicted, Public (Private)</td>
</tr>
<tr>
<td></td>
<td>Public Provision Observed, Public (Private)</td>
<td>Top-Up Provision Observed, Public (Private)</td>
</tr>
<tr>
<td>125</td>
<td>365</td>
<td>365 (0)</td>
</tr>
<tr>
<td></td>
<td>378</td>
<td>351 (8*)</td>
</tr>
<tr>
<td></td>
<td>[358*(1)]*</td>
<td></td>
</tr>
<tr>
<td>275</td>
<td>365</td>
<td>365 (0)</td>
</tr>
<tr>
<td></td>
<td>378</td>
<td>351 (14*)</td>
</tr>
<tr>
<td></td>
<td>[383*(0)]*</td>
<td></td>
</tr>
<tr>
<td>640</td>
<td>365</td>
<td>365 (0)</td>
</tr>
<tr>
<td></td>
<td>378</td>
<td>351 (40*)</td>
</tr>
<tr>
<td></td>
<td>[368*(8)]*</td>
<td></td>
</tr>
<tr>
<td>700</td>
<td>365</td>
<td>365 (10)</td>
</tr>
<tr>
<td></td>
<td>378</td>
<td>351 (46*)</td>
</tr>
<tr>
<td></td>
<td>[342*(19)]*</td>
<td></td>
</tr>
<tr>
<td>1500</td>
<td>365</td>
<td>365 (205)</td>
</tr>
<tr>
<td></td>
<td>378(^T)</td>
<td>[351(210)](^{O,P})</td>
</tr>
<tr>
<td></td>
<td>[318*(113)](^{T,P,*})</td>
<td></td>
</tr>
<tr>
<td>Total Per Person</td>
<td>Public (Private)</td>
<td>365</td>
</tr>
<tr>
<td></td>
<td>172 (123)</td>
<td>378(^T)</td>
</tr>
<tr>
<td></td>
<td>358</td>
<td>[354*(28*)]</td>
</tr>
<tr>
<td>Total</td>
<td>Public (Private)</td>
<td>1825</td>
</tr>
<tr>
<td></td>
<td>860 (617)</td>
<td>1890(^T)</td>
</tr>
<tr>
<td></td>
<td>1790</td>
<td>[1769*(141*)]</td>
</tr>
<tr>
<td>Total</td>
<td>1825</td>
<td>2040</td>
</tr>
<tr>
<td></td>
<td>1890(^T)</td>
<td>2075(^P)</td>
</tr>
<tr>
<td></td>
<td>1910(^*)</td>
<td></td>
</tr>
</tbody>
</table>

Notes: All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value. \(^P\) indicates that there is a statistically significant difference between the top-up or opt-out value and associated public value. \(^{O(T)}\) indicates that there is a statistically significant difference between the observed opt-out (top-up) value for the treatment to which the superscript is attached. All of the entries are rounded to the unit.
<table>
<thead>
<tr>
<th></th>
<th>Sessions with Top-Up</th>
<th>Sessions with Opt-Out</th>
</tr>
</thead>
<tbody>
<tr>
<td>Public-only</td>
<td>Top-Up Predicted</td>
<td>Opt-Out Predicted</td>
</tr>
<tr>
<td>Provision Predicted</td>
<td>Public-only Top-Up</td>
<td>Public-only Top-Up</td>
</tr>
<tr>
<td></td>
<td>Observed</td>
<td>Observed</td>
</tr>
<tr>
<td><strong>Mean Coefficient of Variation (CoV)</strong></td>
<td>0</td>
<td>0.222</td>
</tr>
<tr>
<td><strong>Standard Deviation of CoV</strong></td>
<td>n/a</td>
<td>n/a</td>
</tr>
</tbody>
</table>

Notes: All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value. \(^T\) indicates that there is a statistically significant difference between the top-up or opt-out value and associated public value. \(^O(P)\) indicates that there is a statistically significant difference between the observed opt-out (top-up) value for the treatment to which the superscript is attached.
Table A.3: Per Period Payoffs by Treatment and Income, Last 5 Periods

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>only</td>
<td>Predicted</td>
<td>Predicted</td>
<td>only</td>
<td>Observed</td>
<td>only</td>
</tr>
<tr>
<td>125</td>
<td>979</td>
<td>979</td>
<td>853</td>
<td>986(^T)</td>
<td>943(^P)</td>
<td>972</td>
</tr>
<tr>
<td>275</td>
<td>1112</td>
<td>1112</td>
<td>1035</td>
<td>1115(^T)</td>
<td>1077(^O,P,*)</td>
<td>1107</td>
</tr>
<tr>
<td>640</td>
<td>1346</td>
<td>1346</td>
<td>1354</td>
<td>1340*</td>
<td>1328*</td>
<td>1344*</td>
</tr>
<tr>
<td>700</td>
<td>1377</td>
<td>1378</td>
<td>1398</td>
<td>1371*</td>
<td>1364(^O)</td>
<td>1377(^O)</td>
</tr>
<tr>
<td>1500</td>
<td>1737</td>
<td>1772</td>
<td>1857</td>
<td>1718*</td>
<td>1759(^O)</td>
<td>1741(^O)</td>
</tr>
</tbody>
</table>

Payoff Per Person: 1310, 1317, 1299, 1306\(^T,*\), 1294\(^O,P,*\), 1308\(^O\), 1279\(^P,T,*\)

Total Payoffs: 6550, 6585, 6495, 6522\(^T,*\), 6480\(^O,P,*\), 6541\(^O\), 6395\(^P,T,*\)

Notes: All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value. \(^O(T)\) indicates that there is a statistically significant difference between the top-up or opt-out value and associated public value. \(^O(P)\) indicates that there is a statistically significant difference between the observed opt-out (top-up) value for the treatment to which the superscript is attached. All of the entries are rounded to the unit. The observed top-up mean value of 1364 in the table above is only significantly different from the observed opt-out mean value of 1328 using a Mann-Whitney test and is not significant using a t-test. The observed top-up mean value of 1294 in the table above is only significantly different from the observed public mean value of 1306 using a Mann-Whitney test and is not significant using a t-test. The observed top-up mean value of 1294 in the table above is only significantly different from the observed opt-out mean value of 1279 using a Mann-Whitney test and is not significant using a t-test.
Table A.4: Distributions of per Period Payoffs by Income, Last 5 Periods

<table>
<thead>
<tr>
<th>Public-only Provision</th>
<th>Top-Up Predicted</th>
<th>Opt-Out Predicted</th>
<th>Public-only Provision</th>
<th>Top-Up Observed</th>
<th>Public-only Provision</th>
<th>Opt-Out Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean Coefficient of Variation (CoV)</td>
<td>0.221</td>
<td>0.230</td>
<td>0.296</td>
<td>0.215$^T$</td>
<td>0.244$^P$</td>
<td>0.225</td>
</tr>
<tr>
<td>Standard Deviation of CoV</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>0.015</td>
<td>0.048</td>
<td>0.021</td>
</tr>
</tbody>
</table>

Notes: All statistical tests are conducted using a 10% significance level. * indicates that the observed value is significantly different from its predicted value. $^T$ indicates that there is a statistically significant difference between the top-up or opt-out value and associated public value. $^P$ indicates that there is a statistically significant difference between the observed opt-out (top-up) value for the treatment to which the superscript is attached. The observed CoV value of 0.244 in the above table is only significantly different from the observed public CoV value of 0.210 using a paired t-test and is not significant using a Wilcoxon Sign-Rank test.